

Colligative Properties

1. What is the vapor pressure of an aqueous solution that has 25.0 g of Na_2CO_3 dissolved in 286.00 g of water at 29.0 °C? The vapor pressure of water at 29.0 °C is 30.0 mmHg.

$$P_{\text{soltn.}} = P^\circ \times X_{\text{solvent}}$$

$$25.0 \text{ g Na}_2\text{CO}_3 = 0.236 \text{ mol} \quad 286.00 \text{ g H}_2\text{O} = 15.87 \text{ mol}$$

$$\chi_{\text{H}_2\text{O}} = \frac{15.87 \text{ mol}}{15.87 \text{ mol} + 0.236 \text{ mol}} = 0.985$$

$$P_{\text{soltn.}} = 30.0 \text{ mmHg} \times 0.985 = \mathbf{29.6 \text{ mmHg}}$$

2. Calculate the freezing point of a solution that is prepared by dissolving 1.35 g of aspirin (acetylsalicylic acid, $\text{C}_9\text{H}_8\text{O}_4$) in 100.00 g of chloroform, CHCl_3 . The melting point of CHCl_3 is -63.5 °C and $K_f = 4.70 \text{ }^\circ\text{C}/m$.

$$1.35 \text{ g C}_9\text{H}_8\text{O}_4 = 0.00750 \text{ mol} \quad 100.00 \text{ g CHCl}_3 = 0.10000 \text{ kg}$$

$$m = \frac{0.00750 \text{ mol}}{0.10000 \text{ kg}} = 0.0750 \text{ m}$$

$$K_f = 4.70 \frac{^\circ\text{C}}{m} \times 0.0750 \text{ m} \times 1 = 0.353^\circ\text{C}$$

$$\text{Freezing point} = -63.5^\circ\text{C} - 0.353^\circ\text{C} = \mathbf{-63.9^\circ\text{C}}$$

3. What is the vapor pressure of a solution that contains 8.65 g of urea ($\text{CH}_4\text{N}_2\text{O}$) in 145.25 g of water at 35.0 °C? The vapor pressure of water at 35.0°C is 42.2 mmHg.

$$i = 1 \quad 145.25 \text{ g H}_2\text{O} = 8.06 \text{ mol} \quad 8.65 \text{ g CH}_4\text{N}_2\text{O} = 0.144 \text{ mol}$$

$$P_{\text{soltn.}} = P^\circ \times X_{\text{solvent}}$$

$$\chi_{\text{solvent}} = \frac{8.06 \text{ mol}}{8.06 \text{ mol} + 0.144 \text{ mol}} = 0.982$$

$$P_{\text{soltn.}} = 42.2 \text{ mmHg} \times 0.982 = \mathbf{41.4 \text{ mmHg}}$$

4. A certain sugar is obtained from the degradation of cellulose. A 250.00 mL aqueous solution contains 1.35 g of this sugar. At 28.2 °C, the osmotic pressure is 425.6 mmHg. What is the molar mass of this sugar?

$$425.6 \text{ mmHg} \times \frac{1 \text{ atm}}{760.0 \text{ mmHg}} = 0.5600 \text{ atm} \quad 28.2^\circ\text{C} = 301.35 \text{ K}$$

$$\Pi = MRT \quad \text{solve for } M \quad M = \frac{\Pi}{RT} = \frac{0.5600 \text{ atm}}{0.0821 \frac{\text{L}\cdot\text{atm}}{\text{mol}\cdot\text{K}} \times 301.35 \text{ K}} = 0.0226 \text{ M}$$

$$0.0226 \text{ M} \times 0.25000 \text{ L} = 0.00565 \text{ mol}$$

$$M_m = \frac{1.35 \text{ g}}{0.00565 \text{ mol}} = \mathbf{238.9 \frac{\text{g}}{\text{mol}}} = \mathbf{239 \frac{\text{g}}{\text{mol}}}$$