Wavelength, Frequency, and Energy

1. A laser will emit light with a wavelength of 650 nm. What is the frequency of this light?

$$650 \ nm \times \frac{1 \ m}{10^9 \ nm} = 6.50 \times 10^{-7} \ m$$
$$\nu = \frac{2.998 \times 10^8 \ m/s}{6.50 \times 10^{-7} \ m} = 4.61 \times 10^{14} \ s^{-1}$$

2. The frequency of radiant energy is 5.55×10^{14} Hz. In what region of the electromagnetic spectrum is this? What is the color of the light? (Hint: Calculate the wavelength)

$$\lambda = \frac{c}{v} = \frac{2.998 \times 10^8 \frac{m}{s}}{5.55 \times 10^{14} / s} = 5.40 \times 10^{-7} m = 540 \ nm$$

This is in the visible region and corresponds to the color green.

3. What is the energy, in kJ, of a photon that has a wavelength of 2.46 x 10^2 m?

 $E = \frac{hc}{\lambda} = \frac{(6.626 \times 10^{-34} \, J \cdot s) \times (2.998 \times 10^8 \, m/s)}{2.46 \times 10^2 \, m} = \mathbf{8.08} \times \mathbf{10^{-28}} \, \mathbf{J}$

4. Some sunburn occurs when exposed to light with a wavelength of 325 nm. What is the energy of 1.5 moles of these photons? How many photons are in a 1.50 mJ burst of this radiation?

325 nm = 3.25 x 10⁻⁷ m

$$E = \frac{hc}{\lambda} = \frac{(6.626 \times 10^{-34} J \cdot s) \times (2.998 \times 10^8 m/s)}{3.25 \times 10^{-7} m} = 6.12 \times 10^{-19} J/photon$$
1.5 mol photons $\times \frac{6.02 \times 10^{23} photons}{1 mol photons} \times \frac{6.12 \times 10^{-19} J}{1 photon} = 5.5 \times 10^5 J$
1.50 mJ $\times \frac{1J}{1000 mJ} \times \frac{photon}{6.12 \times 10^{-19} J} = 2.45 \times 10^{15} photons$

5. The work function, Φ , is 437 kJ/mol for copper. What is the threshold frequency? What wavelength does this correspond to?

$$437\frac{kJ}{mol} \times \frac{1000\,J}{1\,kJ} \times \frac{1\,mol}{6.02 \times 10^{23}\,photons} = 7.26 \times 10^{-19}\frac{J}{photon}$$

$$E = hv \text{ and } v = \frac{E}{h} = \frac{7.26 \times 10^{-19} \, J/photon}{6.626 \times 10^{-34} \, J \cdot s} = \mathbf{1.10} \times \mathbf{10^{15}} \, / \mathbf{s}$$
$$\lambda = \frac{2.9998 \times 10^8 \, m/s}{1.10 \times 10^{15} \, / \mathbf{s}} = 2.73 \times 10^7 \, m = \mathbf{273} \, \mathbf{nm}$$